

Percentages – summary

Percentage of a quantity

% means "out of 100" or $\frac{\dots}{100}$ or $\div 100$

e.g. 27% of 152 is $27 \div 100 \times 152 = 41.04$

One number as a % of another

Work out the fraction of the quantity as a decimal then multiply by 100 to transform into a %

e.g. Express 41.04 as a percentage of 152:

$$\frac{41.04}{152} = 41.04 \div 152 = 0.27 \text{ and } 0.27 \times 100 = 27\%$$

Express an increase/decrease as a percentage

Work out the amount the quantity has increased/decreased by express this amount as a percentage of the origin amount

- e.g.
- A price went from £152 to £110.96. What is the % decrease?
 $152 - 110.96 = 41.04$ decrease (out of 152)
 $41.04 \div (\text{out of}) 152 = 0.27$ and $0.27 \times 100 = 27\%$ decrease.
 - A price went from £110.96 to £152. What is the % increase?
 $152 - 110.96 = 41.04$ increase (out of 110.96)
 $41.04 \div (\text{out of}) 110.96 = 0.3699$ and $0.3699 \times 100 = 36.99\%$ increase

Increasing/decreasing using a multiplier

To **increase** an amount by 27%, **multiply** by 1.27
(you effectively work out 127% of the original quantity)
To **decrease** an amount by 27%, **multiply** by 0.73
(you work out what is left: 73% of the original quantity)

- e.g.
- Increase 152 by 27% : $152 \times 1.27 = 193.04$
 - Decrease 152 by 27% : $152 \times 0.73 = 110.96$

Note: Increase or decrease, you MULTIPLY the amount by the multiplier.

Working out the original amount after a percentage change

To work out the original amount, DIVIDE the new amount by the multiplier:
DIVIDE by 1. to retrieve an original amount after an increase
DIVIDE by 0. to retrieve an original amount after a decrease

- e.g.
- After an increase of 27%, an amount has reached £193.04.
What was the original price? $\pounds 193.04 \div 1.27 = \pounds 152$
 - After a decrease of 27%, an amount has reached £110.96
What was the original price? $\pounds 110.96 \div 0.73 = \pounds 152$

Note: Increase or decrease, you DIVIDE the amount by the multiplier.

Repeated % changes. Compound interests

C : the capital (the original amount put in the bank)
 $ab\%$: the (compound) interest *per annum* (*per year*)
 n : the number of years the money stay in the bank
After, n years, the amount in the bank is : $C \times (1.ab)^n$

- e.g. I have £152 in a saving account with interest 27% per annum.
How much money will I have in 7 years?
 $\pounds 152 \times (1.27)^7 = \pounds 809.97$