

## Percentages – summary

### Percentage of a quantity

% means "out of 100" or  $\frac{\dots}{100}$  or  $\div 100$

e.g. 27% of 152 is  $27 \div 100 \times 152 = 41.04$

### One number as a % of another

Work out the fraction of the quantity as a decimal then multiply by 100 to transform into a %

e.g. Express 41.04 as a percentage of 152:

$$\frac{41.04}{152} = 41.04 \div 152 = 0.27 \text{ and } 0.27 \times 100 = 27\%$$

### Express an increase/decrease as a percentage

Work out the amount the quantity has increased/decreased by express this amount as a percentage of the origin amount

- e.g.
- A price went from £152 to £110.96. What is the % decrease?  
 $152 - 110.96 = 41.04$  decrease (out of 152)  
 $41.04 \div (\text{out of}) 152 = 0.27$  and  $0.27 \times 100 = 27\%$  decrease.
  - A price went from £110.96 to £152. What is the % increase?  
 $152 - 110.96 = 41.04$  increase (out of 110.96)  
 $41.04 \div (\text{out of}) 110.96 = 0.3699$  and  $0.3699 \times 100 = 36.99\%$  increase

### Increasing/decreasing using a multiplier

To **increase** an amount by 27%, **multiply** by 1.27  
(you effectively work out 127% of the original quantity)  
To **decrease** an amount by 27%, **multiply** by 0.73  
(you work out what is left: 73% of the original quantity)

- e.g.
- Increase 152 by 27% :  $152 \times 1.27 = 193.04$
  - Decrease 152 by 27% :  $152 \times 0.73 = 110.96$

Note: Increase or decrease, you MULTIPLY the amount by the multiplier.

### Working out the original amount after a percentage change

To work out the original amount, DIVIDE the new amount by the multiplier:  
DIVIDE by 1. .... to retrieve an original amount after an increase  
DIVIDE by 0. .... to retrieve an original amount after a decrease

- e.g.
- After an increase of 27%, an amount has reached £193.04.  
What was the original price?  $\pounds 193.04 \div 1.27 = \pounds 152$
  - After a decrease of 27%, an amount has reached £110.96  
What was the original price?  $\pounds 110.96 \div 0.73 = \pounds 152$

Note: Increase or decrease, you DIVIDE the amount by the multiplier.

### Repeated % changes. Compound interests

$C$  : the capital (the original amount put in the bank)  
 $ab\%$  : the (compound) interest *per annum* (*per year*)  
 $n$  : the number of years the money stay in the bank  
After,  $n$  years, the amount in the bank is :  $C \times (1.ab)^n$

- e.g. I have £152 in a saving account with interest 27% per annum.  
How much money will I have in 7 years?  
 $\pounds 152 \times (1.27)^7 = \pounds 809.97$